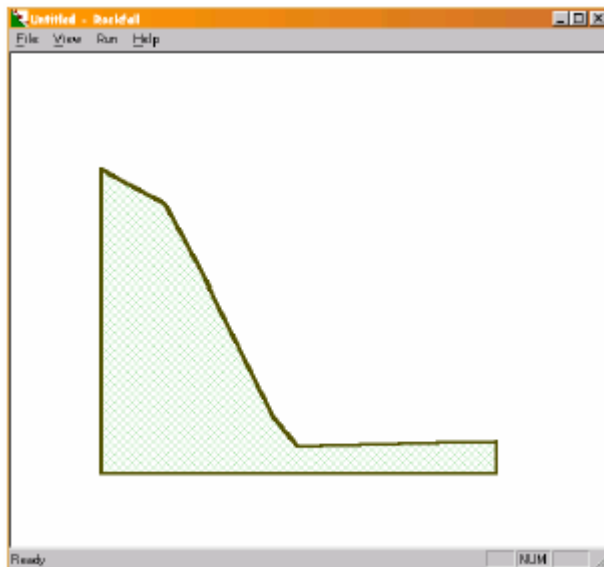


## **SIMULATION OF ROCK FALLS**

**Rockfall** is software which simulates the fall of rock fragments down a slope. The analysis is performed in 2 dimensions and the fragments of the rock are considered as single particles with planar movement which is described by linear components.

The software has a Graphical User Interface and is programmed in Microsoft Visual C ++ 5.

After double-clicking on the rockfall.exe, the following picture appears.



The user can also maximize the application window, so that the full screen is available for viewing the model.

The program operates as a typical Windows program. It has Toolbar Options (File, View, Run, and Help) and in the main screen we can see the cross section of the slope and the fall of the rock fragments.

In order to execute the program the following conditions should be satisfied:

In the directory \WINDOWS\System the user must install the file mfc42.dll, which is usually already there (by the installation of some other program). In the case where this file does not exist, the user can download it (<http://www.microsoft.com>).

Moreover, in the international adjustments of the Windows control panel, the list separator must be defined as the Greek question mark.

## INPUT DATA

In order to define the input data, a Text file must be used. For example, with the help of a text editor like the Windows Notepad, (Start->Programs->Accessories->Notepad).

The input data must be saved as a PCF file, for example data1.rcf.

The structure of the Input Data must be as follows:

-number of points-

x y  $k_n$   $k_s$  f

x y  $k_n$   $k_s$  f

....

For example:

7

0.0 0.0 0.4 0.8 0.35

6.0 -15.32 0.4 0.8 0.2

14.0 -16.00 0.4 0.8 0.35

26.0 -17.3 0.4 0.8 0.3

50.0 -29.3 0.4 0.8 0.32

70.0 -53.2 0.4 0.8 0.35

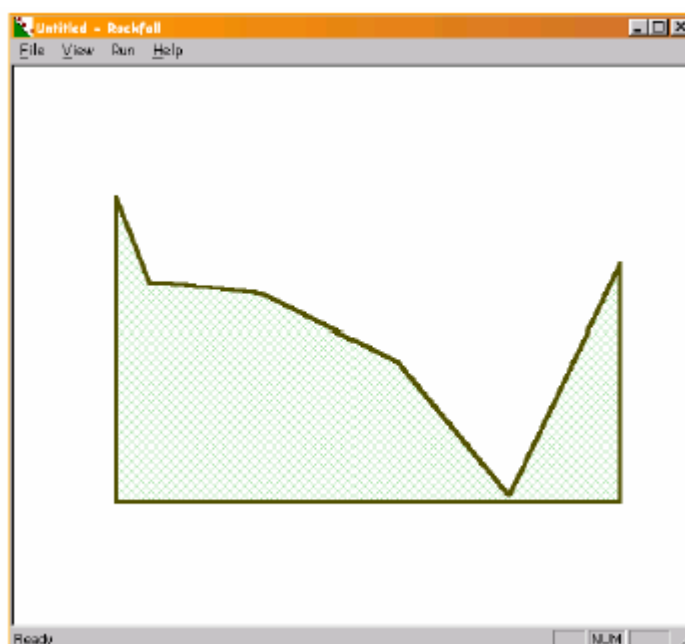
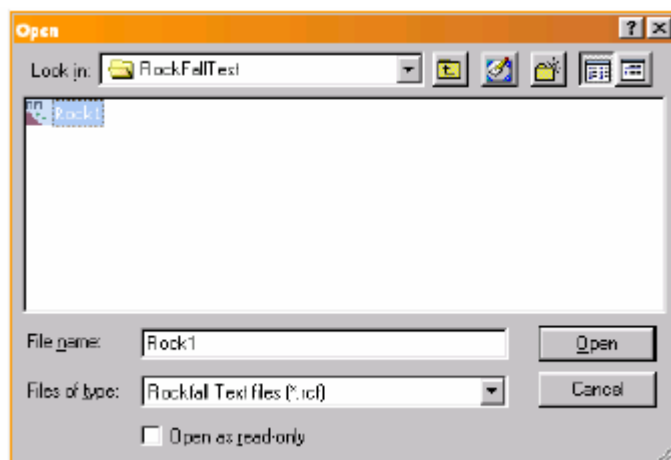
90.0 -12.0 0.4 0.8 0.35

This example describes a polygon slope of 7 points.

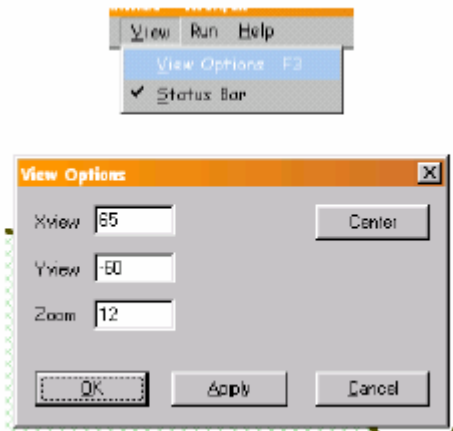
- The first row shows the number of the points. This number must be integer (in this case 7).
- The other rows describe the points and their attributes. The number of these rows is equal to the number of the points which define the slope (7). The values in each row are separated from each other with a simple space, while in order to change from one row to another, the user must press the enter key.
- The values which correspond to “x” must increase as we move downwards to the table. In general, the analysis is performed with the consideration that the rock fragments move with direction to the right.
- The coefficient  $k_n$  is the coefficient of damping towards the normal direction (elastic impact:  $k_n=1$ , complete energy dissipation:  $k_n=0$ ).
- The  $k_s$  coefficient is the coefficient of damping towards the tangent direction.
- The coefficient  $f$  is the friction coefficient and should be selected according to whether sliding or scrolling occurs.

These properties concern the side of the poly-line which begins from the current point. The attributes of the first point concern the first side while the attributes of the last point don't have any participation.

The user must save these values in the form of a .rcf file (e.g. rock1.rcf) and can be recalled through the command File-> Import RCF.



The user can change the appearance of the slope with the command View->View Options, or by pressing the key F3.



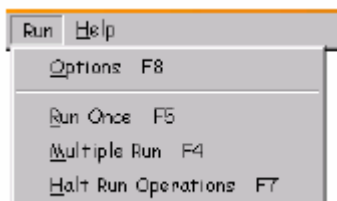
Through this Dialog Window it is feasible to Zoom in or Zoom out. Moreover, it is possible to change the center point of the representation

## **EXECUTION OF THE SIMULATION**

The simulation can be performed by using the 2 following methods:

- Simple Simulation ( Simple Simulation)
- Multiple Simulation ( Multiple Run), mainly for statistical analysis

The user can choose the simulation method through the Run menu.



By clicking the key F8 or Options in the Toolbar Menu appears the following Window:



These are the Simulation Adjustments.

- Ux and Uy describe the initial velocity of the rock fragment in the case of the Simple Simulation (m/sec).
- Umin is the minimum velocity of the rock fragment.

If the velocity of the rock fragment is smaller than  $U_{min}$ , the bouncing ends and the slide or the scrolling begins. The execution of the simulation ends when the velocity of the rock fragment becomes smaller than  $U_{min}$  that is when there is a situation of slide or scrolling and when the friction coefficient is larger than the inclination of the slope.

- Gravity is the acceleration of gravity ( $m/sec^2$ ) and
- $dt$  is the calculation step with recommended values smaller than 0.1 sec.

By clicking in one of the 3 choices of the Run Style, the graphical output of the simulation between the trace of the rock fragments, the in motion rock fragments or the line, change.

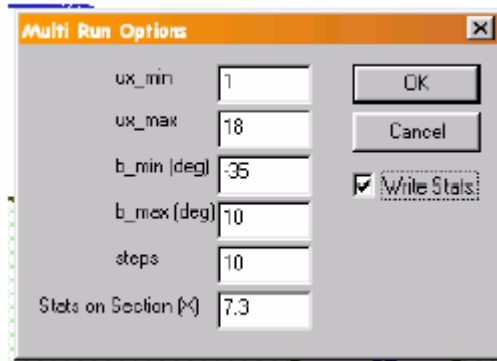
By clicking Run-> Run Once or by pressing the key F5, the user chooses to execute Simple Simulation.



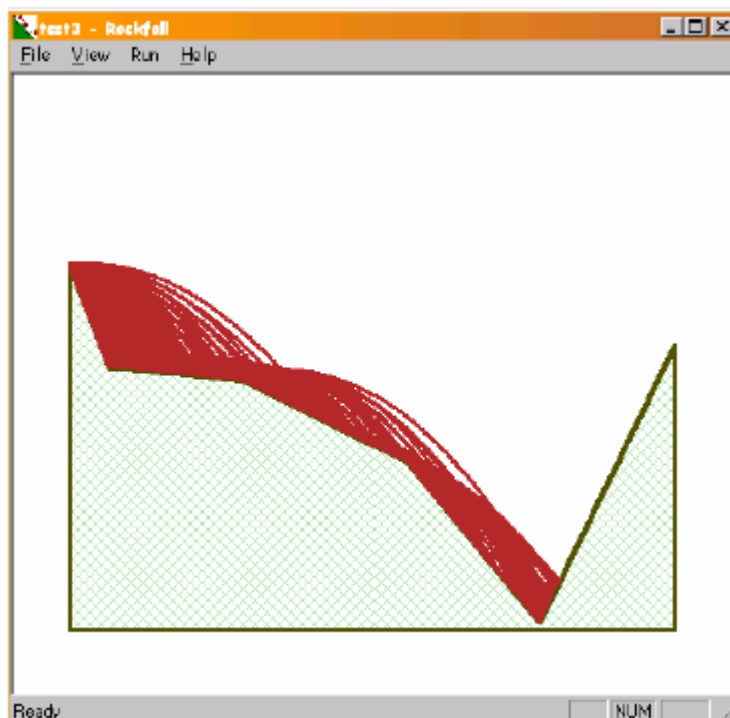
In this graphical output we can see the maximum distance that the rock fragment reaches, the distance where the rock fragments finish, and the real time of the rock fall. By changing the step  $dt$ , it is possible to achieve simulation in “real time”.

In order to terminate the simulation, the user must choose from the run menu, Run->Halt Run Operations or by pressing the key F7.

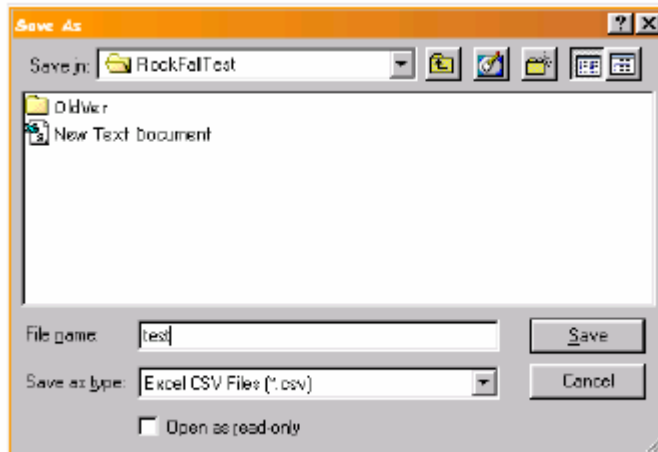
The Statistical Analysis is feasible by using Multiple Run (Menu->Multiple Run) or by pressing the key F4.



- ux\_min , ux\_max is the range of the initial velocity ( m/sec)
- b\_min, b\_max is the range of the initial shot angles (degrees)
- There are executed steps<sup>2</sup> ( for example: 10steps-> 100 simulations)
- The “stats on Xsection” is the position (X) in which the statistics are taken into account for the heigth and the velocity of the rock fragments. When “Write Stats” is on, the statistical is exported in an .xls file. By executing the simulation, appear 100 successive cases of falls for the rock fragment.



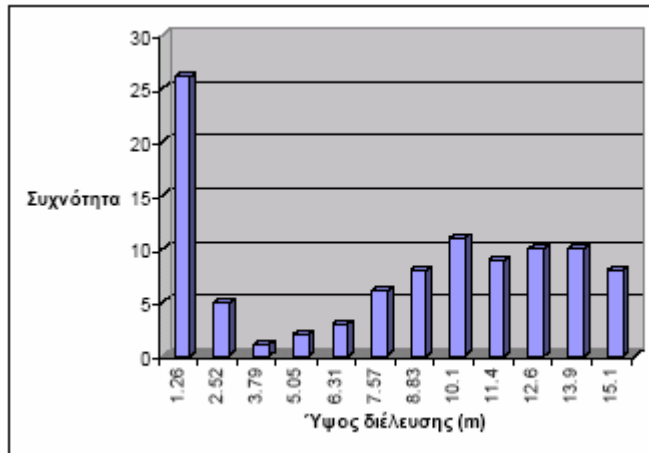
And if the user has selected to export an xls file (Write Stats.), the following Window appears:



The exported file is a CSV file. By opening the file which was created in Excel, appears the following image:

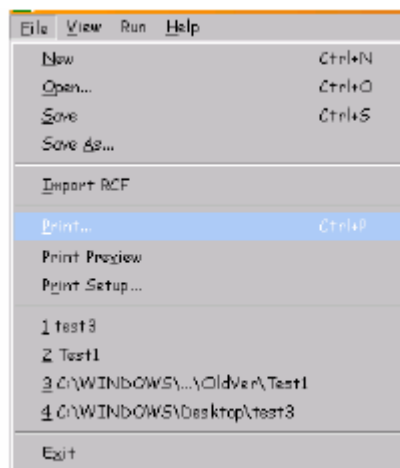
	A	B	C	D	E	F
1	Statistics on 100 falls					
2	10 steps of velocity from 1.000000 m/s to 18.000000 m/s					
3	10 steps of angle from -35.000000 deg to 10.000000 deg					
4						
5	Frequencies of stop distances					
6	Range (m)	Frequency				
7	5.633333	0				
8	11.66667	4				
9	17.5	19				
10	23.33333	11				
11	29.16667	8				
12	35	0				
13	40.83333	0				
14	46.66667	0				
15	52.5	0				
16	58.33333	0				
17	64.16667	0				
18	70	58				
19						
20	Frequencies of max distances					
21	Range (m)	Frequency				

These results can be used and with the help of the Excel the user can have charts:



## **OTHER FUNCTIONS**

From the File menu the user can save a model (Save, Save as.), recall a model (Open), create a new file (New), print (Print) and terminate the program (Exit)





## **BRIEF DISCRIPTION OF THE ALGORITHM- THEORETICAL BASE**

The simulation situation is described by the following parameters :

- Time  $t$
- Function situation:
  - 1: movement in air
  - 2: movement in ground
  - 0: finish of the simulation
- Vector of the position  $[x, y]^T$
- Vector of the velocity  $[u_x, u_y]^T$

The simulation takes place with the execution of 2 loops. In every loop there are calculated the Vector of position and Velocity, according to the calculation step ( $\delta t$ ). Moreover it is calculated the total time  $t_{i+1} = t_i + \delta t$  and the function situation for the next step is ascribed with the execution of the necessary checks

### **Movement in air:**

The movement in air is described with a parabolic trace. The new velocity is given by the following equation:

$$[u_x, u_y]^T = [u_x, u_y - g \delta t]^T$$

While the new position:

$$[x, y]^T = [x + u_x \delta t, y + u_y \delta t - \frac{1}{2} g \delta t^2]^T$$

$g$ : the acceleration of gravity, usually  $9.81 \text{ m/sec}^2$

### **Impact control:**

After calculating the new position of the orbit in air, it is necessary to check the impact with the ground.

**Say**  $(x_1, y_1), (x_2, y_2), \dots, (x_i, y_i), \dots$  are the points which describe the polyline of the surface of the ground. A control takes place for all of the sides of the ground

If  $x_i \leq x \leq x_{i+1}$

Then for the side “ $i+1$ ” the following check takes place:

First of all the magnitude  $y_0$  is calculated:

$$y_0 = \frac{y_{i+1} - y_i}{x_{i+1} - x_i} (x - x_i) + y_i$$

- If  $y > y_0$ , then the rock fragment is still on air (situation number “1”)
- If  $y \leq y_0$ , then the impact has allready occurred and the current step  $\delta t$  is been recalled:

$$\begin{aligned} [ux, uy]^T &= [ux, uy + g \delta t]^T \\ [x, y]^T &= [x - ux \delta t, y - uy \delta t + \frac{1}{2} g \delta t^2]^T \end{aligned}$$

By solving the quadratic equation, the appropriate  $\delta t'$  is being calculated so that it will be executed again with step  $\delta t'$  which will cause:  
 $y=y_0$  (the rock fragment is on the ground)

At this point the tangent and the vertical components of the velocity on the ground are being calculated. If the inclination angle of the ground is  $\theta$ , then:

$$\begin{pmatrix} u_s \\ u_n \end{pmatrix} = \begin{pmatrix} \cos\theta & \sin\theta \\ -\sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} u_x \\ u_y \end{pmatrix}$$

During the impact, a portion of the kinetic energy is being absorbed due to the inelastic impact. Towards the tangent component the direction of the velocity is stable while the value is being reduced by a coefficient  $k_s$ . When the damping coefficient is 1, then the absorption of the kinetic energy is zero, while when the damping coefficient is 0, all the kinetic energy is being absorbed. Towards the vertical component, we have inelastic impact. The reduction of the kinetic energy is being calculated with the help of the  $k_n$  coefficient. The new values of the velocity are:

$$[u_s', u_n']^T = [k_s u_s, -k_n u_n]^T$$

$$\begin{pmatrix} u_x \\ u_y \end{pmatrix} = \begin{pmatrix} \cos\theta & -\sin\theta \\ \sin\theta & \cos\theta \end{pmatrix} \begin{pmatrix} u_s' \\ u_n' \end{pmatrix}$$

### **Checking the alteration of the situation:**

Checking the alteration of the situation, according to the vertical component of the velocity:

If  $|u_n| > u_{\min}$ , then the simulation continues in the situation number "1"

If  $|u_n| < u_{\min}$ , then the simulation continues in the situation number "2", movement in the ground. By placing  $u_n = 0$ ,  $u_x, u_y$  are being anew calculated.

### **Movement on the ground :**

The movement on the ground is a linear accelerated one with resistance due to the friction or due to resistance in scrolling. This is expressed by a dimensionless coefficient "f". If N is the vertical reaction that the ground forces on the rock fragment, then the resistance in moving equals with  $fN$ . The coefficient should be chosen by the user according to whether it is expected sliding or scrolling, according to the shape of the rock fragments, the inclination of the ground and the friction coefficient in sliding.

### **Side localization**

If  $x_i \leq x \leq x_{i+1}$

Then the movement takes place on the side “ $i-i+1$ ”

The inclination of the side is being calculated

$$\lambda = \frac{y_{i+1} - y_i}{x_{i+1} - x_i}$$

the angle:  $\theta = \tan^{-1}\lambda$

### **Termination of the simulation**

If the situation is number “2”,  $\sqrt{u_x^2 + u_y^2} \leq u_{\min}$  and the resistance coefficient is larger than the ground inclination : ( $f > |\lambda|$ ), then the simulation is being terminated.

### **Movement on the ground:**

The linear accelerated movement takes place according to the acceleration components  $\alpha_x, \alpha_y$ .

$$\alpha_x = -g \sin\theta \cos\theta - g \cos\theta \cos\theta f_{<s>}$$

$$\alpha_y = -g \sin\theta \sin\theta - g \cos\theta \sin\theta f_{<s>}$$

The <s> coefficient equals :

$$\mathbf{1} \text{ when } u_x > 0$$

$$\mathbf{-1} \text{ when } u_x < 0$$

$$\mathbf{0} \text{ when } u_x = 0$$

The new value of the velocity is calculated by the following equation:

$$[u_x, u_y]^T = [u_x + \alpha_x \delta t, u_y + \alpha_y \delta t]^T$$

While the new position:

$$[x, y]^T = [x + u_x \delta t + \frac{1}{2} \alpha_x \delta t^2, y + u_y \delta t + \frac{1}{2} \alpha_y \delta t^2]^T$$

In some cases though, the escapement is unacceptable and therefore an additional check must take place concerning the direction of the old and the new  $u_x$  component. In the case where the direction is different, then the calculations take place not by using  $\delta t$  but with,

$$\delta t' = -u_x / \alpha_x$$

### **Situation alteration check:**

This check takes place to define whether the new x position is between the side

“ $i-i+1$ ” or not:

$$x_i \leq x \leq x_{i+1}$$

If so, then the simulation continues in the situation “2”. If not, then the appropriate  $\delta t$  is being calculated so that the rock fall will be within this limit.

And the situation changes to 1 so as in the next loop to implement movement in the air, or impact according to the ground’s morphology.

### **Additional termination checks:**

In the case where the rock fragment finds itself beyond the ground limits, then the simulation is being terminated.

In the case where the total simulation time exceeds  $t=40$  sec then the simulation is being terminated.

Finally, in the case where the rock fragments move on the ground, in cavity with a shape like a V, then the simulation is being terminated in order to avoid the creation of an interminable loop.